

01) Números naturais múltiplos de 4 entre 150 e 1000:
(152, 156, 160, ..., 996)

a) $a_n = a_1 + (n - 1) \cdot r$
 $996 = 152 + (n - 1) \cdot 4$
 $n = 212$ números serão exibidos na tela do computador.

b) $S_n = \frac{(a_1 + a_n) \cdot n}{2}$
 $S_{212} = \frac{(152 + 996) \cdot 212}{2}$
 $S_{212} = 121688$

Soma = 121688

02) Usaremos o Princípio Fundamental da Contagem.

Número de senhas com 6 caracteres:

K V V A A A

$$1 \times 5 \times 4 \times 10 \times 10 \times 10 = 20000$$

Número de senhas com 7 caracteres:

K V V A A A A

$$1 \times 5 \times 4 \times 10 \times 10 \times 10 \times 10 = 200000$$

Número de senhas com 8 caracteres:

K V V A A A A A

$$1 \times 5 \times 4 \times 10 \times 10 \times 10 \times 10 \times 10 = 2000000$$

Total de senhas que satisfazem as exigências de Keli:

$$20000 + 200000 + 2000000 = 2220000 \text{ senhas}$$

03)
$$\begin{cases} \textcircled{1} & x + y + z = 0 \\ \textcircled{2} & 2x - y - 2z = 5 \\ \textcircled{3} & 5x + 4y + 3z = 1 \end{cases}$$

$$\begin{array}{l} -2 \textcircled{1} + \textcircled{2} \Rightarrow \\ -5 \textcircled{1} + \textcircled{3} \end{array} \Rightarrow \begin{cases} -3y - 4z = 5 \\ -y - 2z = 1 \quad (-2) \end{cases}$$

$$+ \begin{cases} -3y - 4z = 5 \\ 2y + 4z = -2 \end{cases}$$

$$-y = 3$$

$$y = -3$$

$$\begin{array}{l} -y - 2z = 1 \\ -(-3) - 2z = 1 \\ -3 - 2z = 1 \\ -2z = 1 + 3 \\ z = -2 \end{array}$$

$$x + y + z = 0 \Rightarrow x - 3 - 2 = 0 \\ x = 5$$

$$\begin{cases} \textcircled{1} & x + y + z = 0 \\ \textcircled{2} & 2x - y - 2z = 5 \\ \textcircled{3} & 5x + 4y + 3z = 1 \end{cases}$$

$$\begin{aligned} -y - 2z &= 1 \\ 3 - 2z &= 1 \\ -2z &= 1 - 3 \\ z &= 1 \end{aligned}$$

$$\begin{aligned} -2 \textcircled{1} + \textcircled{2} &\Rightarrow \begin{cases} -3y - 4z = 5 \\ -y - 2z = 1 \quad (-2) \end{cases} \\ -5 \textcircled{1} + \textcircled{3} & \begin{cases} -3y - 4z = 5 \\ 2y + 4z = -2 \end{cases} \\ &+ \begin{cases} -3y - 4z = 5 \\ 2y + 4z = -2 \end{cases} \\ &\quad -y = 3 \\ &\quad y = -3 \end{aligned}$$

$$\begin{aligned} x + y + z &= 0 \\ x - 3 + 1 &= 0 \\ x &= 2 \end{aligned}$$

$$S = \{(2, -3, 1)\}$$

$$\begin{vmatrix} 2z & -y & -x-y \\ x-2z & z & y+3z \\ x-y & 3z & x-z \end{vmatrix} = \begin{vmatrix} 2 & 3 & 1 \\ 0 & 1 & 0 \\ 5 & 3 & 1 \\ 2 & 3 & 1 \\ 0 & 1 & 0 \end{vmatrix} = 2 - 5 = -3$$

04) a) $A \stackrel{N}{=} \tau_F$

$$\tau_F = \frac{4 \cdot 40}{2}$$

$$\tau_F = 80 \text{ J}$$

b) $A \stackrel{N}{=} \tau_F$

$$\tau_F = \frac{4 \cdot 40}{2} + 1 \cdot 40 + \frac{1 \cdot 40}{2} + \frac{1 \cdot (-40)}{2} + 1 \cdot (-40) + \frac{1(-40)}{2}$$

$$\tau_F = 60 \text{ J}$$

c) $\tau_{FR} = \Delta E_c$

$$\tau_{FR} = \frac{mv^2}{2} - \frac{mv_0^2}{2}$$

$$120 = \frac{1,2 \cdot v^2}{2}$$

$$v^2 = 200$$

$$v = 10\sqrt{2} \text{ m/s}$$

05) a) $Q = Q_{S_G} + Q_{L_G} + Q_{S_A} + Q_{L_A}$
 $Q = m \cdot c_G \cdot \Delta T_G + mL_F + m \cdot c_A \cdot \Delta T_A + mL_V$
 $Q = 100 \cdot 0,55 \cdot (0 - (-5)) + 100 \cdot 80 + 100 \cdot 1 \cdot (100 - 0) + 100 \cdot 540$
 $Q = 275 + 8000 + 10000 + 54000$
 $Q = 72275 \text{ cal}$

b) $Q_F + Q_A = 0$

$$m_F \cdot c_P \cdot \Delta T_F + m_A \cdot c_A \cdot \Delta T_A = 0$$

$$20 \cdot 0,11 \cdot (T - 500) + 100 \cdot 1 \cdot (T - 20) = 0$$

$$2,2T - 1100 + 100T - 2000 = 0$$

$$102T = 3300$$

$$T = \frac{3300}{102}$$

$$T = 32,35 \text{ }^\circ\text{C}$$

c) Gelo

$$Q = m \cdot L$$

$$Q = 10 \cdot 80$$

$$Q = 800 \text{ cal}$$

Álcool (sólido)

$$Q = m \cdot L$$

$$Q = 10 \cdot 25$$

$$Q = 250 \text{ cal}$$

Mercúrio (sólido)

$$Q = m \cdot L$$

$$Q = 10 \cdot 2,8$$

$$Q = 28 \text{ cal}$$

Nitrogênio (sólido)

$$Q = m \cdot L$$

$$Q = 10 \cdot 6,1$$

$$Q = 61 \text{ cal}$$

Prata

$$Q = m \cdot L$$

$$Q = 10 \cdot 21$$

$$Q = 210 \text{ cal}$$

Chumbo

$$Q = m \cdot L$$

$$Q = 10 \cdot 5,8$$

$$Q = 58 \text{ cal}$$

Ferro

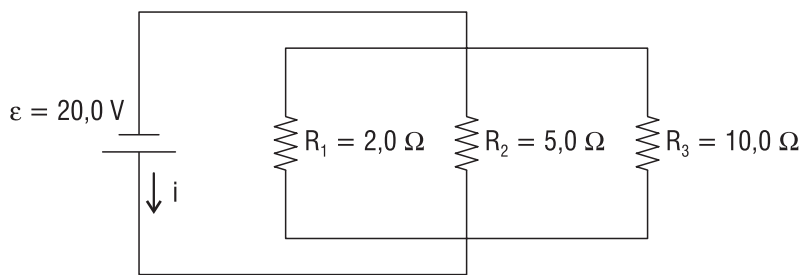
$$Q = m \cdot L$$

$$Q = 10 \cdot 64$$

$$Q = 640 \text{ cal}$$

As substâncias totalmente fundidas são: mercúrio, nitrogênio e chumbo, pois as 100 calorias fornecidas são maiores do que a quantidade de calor necessária para fundi-las

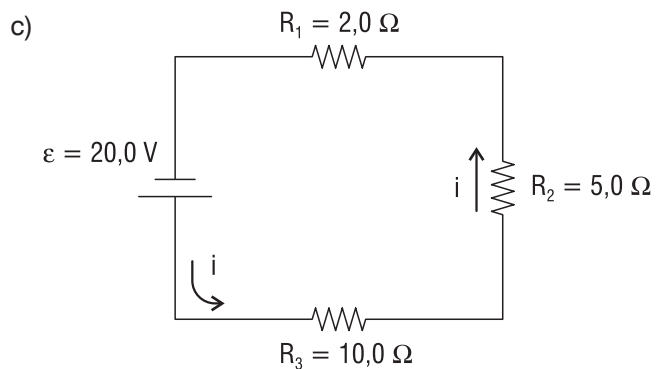
06)



$$\begin{aligned} \text{a) } \frac{1}{R_{\text{EQ}}} &= \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} & i &= \frac{\varepsilon}{R_{\text{EQ}}} \\ \frac{1}{R_{\text{EQ}}} &= \frac{1}{2,0} + \frac{1}{5,0} + \frac{1}{10,0} & i &= \frac{20,0}{10,0} \\ \frac{1}{R_{\text{EQ}}} &= \frac{8,0}{10,0} & i &= \frac{20,0}{8,0} \\ R_{\text{EQ}} &= \frac{10,0}{8,0} \, \Omega & i &= 16 \text{ A} \end{aligned}$$

$$\begin{aligned} \text{b) } P_{R_2} &= \frac{\varepsilon^2}{R_2} \\ P_{R_2} &= \frac{(20,0)^2}{5,0} \Rightarrow P_{R_2} = 80 \text{ W} \end{aligned}$$

$$\begin{aligned} P_{R_3} &= \frac{\varepsilon^2}{R_3} \\ P_{R_3} &= \frac{(20,0)^2}{10} \Rightarrow P_{R_3} = 40 \text{ W} \end{aligned}$$



$$\begin{aligned} R_{\text{EQ}} &= R_1 + R_2 + R_3 \\ R_{\text{EQ}} &= 17,0 \, \Omega \end{aligned}$$

$$\begin{aligned} i &= \frac{\varepsilon}{R_{\text{EQ}}} \\ i &= \frac{20,0}{17,0} \\ i &= 1,18 \text{ A} \end{aligned}$$

$$\begin{aligned} P_2 &= R_2 \cdot I^2 \\ P_2 &= 5,0 \cdot (1,18)^2 \\ P_2 &= 6,96 \text{ W} \end{aligned}$$