

$$01) |A| = \cos(x) \cdot \cos(y) \cdot \operatorname{sen}\left(y, \frac{\pi}{2}\right)$$

$$* \operatorname{sen}\left(y, \frac{\pi}{2}\right) = \operatorname{sen}(y) \cdot \cos\left(\frac{\pi}{2}\right) + \operatorname{sen}\left(\frac{\pi}{2}\right) \cdot \cos(y) = \cos(y)$$

$$|A| = \cos(x) \cdot \cos^2(y)$$

$$|B| = \cos^2(y) \cdot \operatorname{sen}(x)$$

$$|C| = \operatorname{sen}^2(x) \cdot \cos(y) \cdot \operatorname{sen}(y) + \cos^2(x) \cdot \operatorname{sen}(y) \cdot \cos(y)$$

$$|C| = \cos(y) \cdot \operatorname{sen}(y) \cdot [\operatorname{sen}^2(x) + \cos^2(x)]$$

$$|C| = \cos(y) \cdot \operatorname{sen}(y)$$

$$|A|^2 = \cos^2(x) \cdot \cos^4(y)$$

$$|B|^2 = \operatorname{sen}^2(x) \cdot \cos^4(y)$$

$$|C|^2 = \cos^2(y) \cdot \operatorname{sen}^2(y)$$

$$\sqrt{|A|^2 + |B|^2 + |C|^2} = \sqrt{\cos^2(x) \cdot \cos^4(y) + \operatorname{sen}^2(x) \cdot \cos^4(y) + \cos^2(y) \cdot \operatorname{sen}^2(y)}$$

$$= \sqrt{\cos^4(y) [\cos^2(x) + \operatorname{sen}^2(x)] + \cos^2(y) \cdot \operatorname{sen}^2(y)}$$

$$= \sqrt{\cos^4(y) \cdot 1 + \cos^2(y) \cdot \operatorname{sen}^2(y)}$$

$$= \sqrt{\cos^2(y) [\cos^2(y) + \operatorname{sen}^2(y)]}$$

$$= \sqrt{\cos^2(y)} = |\cos(y)|$$

02) Ponto de intersecção da reta  $y - 2x + 7 = 0$  com o eixo das ordenadas.

$$x = 0$$

$$y = -7$$

Focos da hipérbole:

$$\frac{x^2}{4} - \frac{y^2}{12} = 1$$

Eixo real horizontal e centro (0, 0)

$$a^2 = 4 \text{ e } b^2 = 12$$

$$c^2 = a^2 + b^2$$

$$c^2 = 16$$

$$c = 4$$

Focos:  $F_1(-4, 0)$  e  $F_2(4, 0)$

Parábola:  $y = ax^2 + bx + c$

Passa por (0, -7)  $\rightarrow c = -7$

Passa por (-4, 0) e (4, 0)  $\rightarrow$  As raízes são  $x = -4$  e  $x = 4$

Usando as relações de Girard:

$$\frac{a}{c} = -16 \rightarrow \frac{-7a}{c} = -16 \rightarrow a = \frac{7}{16}$$

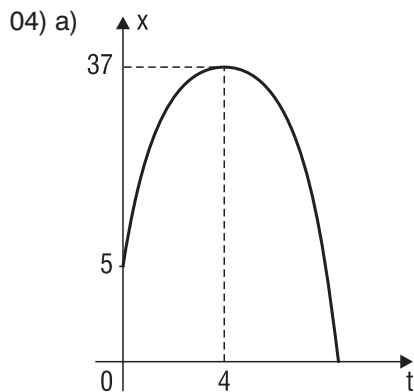
$$\frac{-b}{a} = 0 \rightarrow b = 0$$

$$\text{Parábola: } y = \frac{7}{16}x^2 - 7$$

$$03) V_{\text{Tetraedro}} = A_{\text{Base}} \cdot \frac{h}{3}$$

$$V_{\text{Tetraedro}} = \left[ \left( \frac{x}{2} \right) \cdot \left( \frac{x}{2} \right) \cdot \left( \frac{1}{2} \right) \right] \cdot \left( \frac{x}{2} \right) \cdot \left( \frac{1}{3} \right)$$

$$V_{\text{Tetraedro}} = \left( \frac{x^3}{48} \right) \text{ u.v.}$$



b)  $v = v_0 + a \cdot t$   
 $v = 16 - 4 \cdot 4$   
 $v = 0$

c) Aos 4 s, a bola pára e retorna. Logo, temos:

$t = 4 \text{ s}$	$t = 5 \text{ s}$
$x = 5 + 16 \cdot t - 2t^2$	$x = 5 + 16 \cdot t - 2t^2$
$x = 5 + 16 \cdot 4 - 2 \cdot 4^2$	$x = 5 + 16 \cdot 5 - 2 \cdot 5^2$
$x = 5 + 64 - 32$	$x = 5 + 80 - 50$
$x = 37 \text{ m}$	$x = 35 \text{ m}$

Distância percorrida  
34 m

Deslocamento  
30 m

05) a)  $\Delta U = Q - W$   
 $Q = \Delta U + W$   
 $Q = \Delta U + P \cdot \Delta V$   
 $Q = 1000 + 10^5 \cdot 50 \cdot 10^{-4}$   
 $Q = 1000 + 500$   
 $Q = 1500 \text{ J}$

b) Por se tratar de uma transformação isovolumétrica, o trabalho termodinâmico é nulo.

c) Em uma transformação isovolumétrica, tem-se:

$$\frac{p_B}{T_B} = \frac{p_C}{T_C}$$

$$\frac{10^5}{350} = \frac{p_C}{700}$$

$$p_C = 2 \cdot 10^5 \text{ N/m}^2$$

06) a)  $E_p = q \cdot V$   
 $0,0006 = 10^{-6} \cdot V$   
 $6 \cdot 10^{-4} = 10^{-6} \cdot V$   
 $V = 6 \cdot 10^2 \text{ V}$

b)  $W = -\Delta E_p$   
 $W = -(0,0004 - 0,001)$   
 $W = -(-0,0006)$   
 $W = 0,0006 \text{ J}$

